

Stochastic Processes and Probability Theory III  
**Assignment #5. Due Wednesday, June 3**

1. Let  $P_{ij} = \frac{e^{-i} i^j}{j!}$ ,  $i, j = 0, 1, \dots$  be the transition probabilities for a Markov chain  $X_n$ . We consider  $P_{00} = 1$ . Verify that  $X_n$  is a martingale.
2. Let  $X_n$  be a Markov chain whose transition probabilities are  $P_{ij} = \frac{1}{e(j-i)!}$  for  $i = 0, 1, \dots$  and  $j = i, i + 1, \dots$ . Verify the martingale property for
  - (a)  $Y_n = X_n - n$
  - (b)  $U_n = Y_n^2 - n$
  - (c)  $V_n = e^{X_n - n(e-1)}$
3. Problem 35.1 from the text
4. Problem 35.6 from the text.