

STAT 244BU Hw 5 Answer Key

7. a.

Source of Variation	Sum of Squares	Degrees of Freedom	Mean Square	<i>F</i>	<i>p</i> -value
Treatments	4560	2	2280	9.87	.0006
Error	6240	27	231.11		
Total	10800	29			

b. Using *F* table (2 degrees of freedom numerator and 27 denominator), *p*-value is less than .01

Using Excel or Minitab, the *p*-value corresponding to *F* = 9.87 is .0006.

Because *p*-value ≤ α = .05, we reject the null hypothesis that the means of the three assembly methods are equal.

9.

	50°	60°	70°
Sample Mean	33	29	28
Sample Variance	32	17.5	9.5

$$\bar{\bar{x}} = (33 + 29 + 28)/3 = 30$$

$$SSTR = \sum_{j=1}^k n_j (\bar{x}_j - \bar{\bar{x}})^2 = 5(33 - 30)^2 + 5(29 - 30)^2 + 5(28 - 30)^2 = 70$$

$$MSTR = SSTR / (k - 1) = 70 / 2 = 35$$

$$SSE = \sum_{j=1}^k (n_j - 1)s_j^2 = 4(32) + 4(17.5) + 4(9.5) = 236$$

$$MSE = SSE / (n_T - k) = 236 / (15 - 3) = 19.67$$

$$F = MSTR / MSE = 35 / 19.67 = 1.78$$

Using *F* table (2 degrees of freedom numerator and 12 denominator), *p*-value is greater than .10

Using Excel or Minitab the *p*-value corresponding to *F* = 1.78 is .2104.

Because p -value $> \alpha = .05$, we cannot reject the null hypothesis that the mean yields for the three temperatures are equal.

17. a.

	Marketing Managers	Marketing Research	Advertising
Sample Mean	5	4.5	6
Sample Variance	.8	.3	.4

$$\bar{\bar{x}} = (5 + 4.5 + 6)/3 = 5.17$$

$$SSTR = \sum_{j=1}^k n_j (\bar{x}_j - \bar{\bar{x}})^2 = 6(5 - 5.17)^2 + 6(4.5 - 5.17)^2 + 6(6 - 5.17)^2 = 7.00$$

$$MSTR = SSTR / (k - 1) = 7.00/2 = 3.5$$

$$SSE = \sum_{j=1}^k (n_j - 1)s_j^2 = 5(.8) + 5(.3) + 5(.4) = 7.50$$

$$MSE = SSE / (n_T - k) = 7.50/(18 - 3) = .5$$

$$F = MSTR / MSE = 3.5/.50 = 7.00$$

Using F table (2 degrees of freedom numerator and 15 denominator), p -value is less than .01

Using Excel or Minitab, the p -value corresponding to $F = 7.00$ is .0071

Because p -value $\leq \alpha = .05$, we reject the null hypothesis that the mean perception score is the same for the three groups of specialists.

b. Since there are only 3 possible pairwise comparisons we will use the Bonferroni adjustment.

$$= .05/3 = .017$$

$t_{.017/2} = t_{.0085}$ which is approximately $t_{.01} = 2.602$

$$BSD = 2.602 \sqrt{MSE \left(\frac{1}{n_i} + \frac{1}{n_j} \right)} = 2.602 \sqrt{.5 \left(\frac{1}{6} + \frac{1}{6} \right)} = 1.06$$

$$|\bar{x}_1 - \bar{x}_2| = |5 - 4.5| = .5 < 1.06; \text{ no significant difference}$$

$$|\bar{x}_1 - \bar{x}_3| = |5 - 6| = 1 < 1.06; \text{ no significant difference}$$

$$|\bar{x}_2 - \bar{x}_3| = |4.5 - 6| = 1.5 > 1.06; \text{ significant difference}$$

25. The prices were entered into column 1 of the Minitab worksheet. Coding the treatments as 1 for CVS, 2 for Kmart, 3 for Rite-Aid, and 4 for Wegmans, the coded values were entered into column 2. Finally, the corresponding number of each item was entered into column 3. The Minitab output is shown below:

Two-way ANOVA: Price versus Block, Treatment

Source	DF	SS	MS	F	P
Block	12	323.790	26.9825	63.17	0.000
Treatment	3	9.802	3.2672	7.65	0.000
Error	36	15.376	0.4271		
Total	51	348.968			

$$S = 0.6535 \quad R\text{-Sq} = 95.59\% \quad R\text{-Sq}(\text{adj}) = 93.76\%$$

The p -value corresponding to Treatment is 0.000; because the p -value $< \alpha = .05$, there is a significant difference in the mean price for the four retail outlets.

31. Factor A is method of loading and unloading; Factor B is type of ride.

		Factor B			Factor A
		Roller Coaster	Screaming Demon	Log Flume	Means
Factor A	Method 1	$\bar{x}_{11} = 42$	$\bar{x}_{12} = 48$	$\bar{x}_{13} = 48$	$\bar{x}_{1\cdot} = 46$
	Method 2	$\bar{x}_{21} = 50$	$\bar{x}_{22} = 48$	$\bar{x}_{23} = 46$	$\bar{x}_{2\cdot} = 48$
Factor B	Means	$\bar{x}_{\cdot 1} = 46$	$\bar{x}_{\cdot 2} = 48$	$\bar{x}_{\cdot 3} = 47$	$\bar{\bar{x}} = 47$

Step 1

$$SST = \sum_i \sum_j \sum_k (x_{ijk} - \bar{\bar{x}})^2 = (41 - 47)^2 + (43 - 47)^2 + \dots + (44 - 47)^2 = 136$$

Step 2

$$SSA = br \sum_i (\bar{x}_{i0} - \bar{\bar{x}})^2 = 3 (2) [(46 - 47)^2 + (48 - 47)^2] = 12$$

Step 3

$$SSB = ar \sum_j (\bar{x}_{0j} - \bar{\bar{x}})^2 = 2 (2) [(46 - 47)^2 + (48 - 47)^2 + (47 - 47)^2] = 8$$

Step 4

$$SSAB = r \sum_i \sum_j (\bar{x}_{ij} - \bar{x}_{i0} - \bar{x}_{0j} + \bar{\bar{x}})^2 = 2 [(41 - 46 - 46 + 47)^2 + \dots + (44 - 48 - 47 + 47)^2] =$$

56

Step 5

$$SSE = SST - SSA - SSB - SSAB = 136 - 12 - 8 - 56 = 60$$

Source of Variation	Sum of Squares	Degrees of Freedom	Mean Square	F	p-value
Factor A	12	1	12	12/10 = 1.2	.3153
Factor B	8	2	4	4/10 = .4	.6870
Interaction	56	2	28	28/10 = 2.8	.1384
Error	60	6	10		
Total	136	11			

Using F table for Factor A (1 degree of freedom numerator and 6 denominator), p-value is greater than .10

Using Excel or Minitab, the p-value corresponding to F = 1.2 is .3153.

Because p-value > $\alpha = .05$, Factor A is not significant

Using F table for Factor B (2 degrees of freedom numerator and 6 denominator), p-value is greater than .10

Using Excel or Minitab, the p -value corresponding to $F = .4$ is .6870.

Because p -value $> \alpha = .05$, Factor B is not significant

Using F table for Interaction (2 degrees of freedom numerator and 6 denominator), p -value is greater than .10

Using Excel or Minitab, the p -value corresponding to $F = 2.8$ is .1384.

Because p -value $> \alpha = .05$, Interaction is not significant

33. Factor A is time pressure (low and moderate); Factor B is level of knowledge (naïve, declarative and procedural).

$$\bar{x}_{11} = (1.13 + 1.56 + 2.00)/3 = 1.563$$

$$\bar{x}_{21} = (0.48 + 1.68 + 2.86)/3 = 1.673$$

$$\bar{x}_{12} = (1.13 + 0.48)/2 = 0.805$$

$$\bar{x}_{22} = (1.56 + 1.68)/2 = 1.620$$

$$\bar{x}_{13} = (2.00 + 2.86)/2 = 2.43$$

$$\bar{\bar{x}} = (1.13 + 1.56 + 2.00 + 0.48 + 1.68 + 2.86)/6 = 1.618$$

Step 1

SST = 327.50 (given in problem statement)

Step 2

$$SSA = br \sum_i (\bar{x}_{i0} - \bar{\bar{x}})^2 = 3(25)[(1.563 - 1.618)^2 + (1.673 - 1.618)^2] = 0.4538$$

Step 3

$$SSB = ar \sum_j (\bar{x}_{0j} - \bar{\bar{x}})^2 = 2(25)[(0.805 - 1.618)^2 + (1.62 - 1.618)^2 + (2.43 - 1.618)^2] = 66.0159$$

Step 4

$$SSAB = r \sum_i \sum_j (\bar{x}_{ij} - \bar{x}_{i0} - \bar{x}_{0j} + \bar{\bar{x}})^2 = 25[(1.13 - 1.563 - 0.805 + 1.618)^2 + (1.56 - 1.563 - 1.62 + 1.618)^2 + \dots + (2.86 - 1.673 - 2.43 + 1.618)^2] = 14.2525$$

Step 5

$$SSE = SST - SSA - SSB - SSAB = 327.50 - 0.4538 - 66.0159 - 14.2525$$

Source of Variation	Sum of Squares	Degrees of Freedom	Mean Square	F	p-value
Factor A	0.4538	1	0.4538	0.2648	.6076
Factor B	66.1059	2	33.0080	19.2608	.0000
Interaction	14.2525	2	7.1263	4.1583	.0176
Error	246.7778	144	1.7137		
Total	327.5000	149			

Factor A: Using Excel or Minitab, the p -value corresponding to $F = .2648$ is $.6076$. Because p -value $> \alpha = .05$, Factor A is not significant.

Factor B: Using Excel or Minitab, the p -value corresponding to $F = 19.2608$ is $.0000$. Because p -value $\leq \alpha = .05$, Factor B is significant.

Interaction: Using Excel or Minitab, the p -value corresponding to $F = 4.1583$ is $.0176$. Because p -value $\leq \alpha = .05$, Interaction is significant.